

## ORIGINAL ARTICLE

# Assessing reduction of cluster size to estimate wood volume in an Amazonian forest

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## ABSTRACT

While the Brazilian National Forest Inventory (NFI) is in progress, there is a growing demand to understand the effect of cluster size on the accuracy and precision of forest-attribute estimation. We aimed to find the minimum cluster size (in area) to estimate merchantable volume (MV) with the same accuracy and precision as the estimates derived from the original cluster of 8,000 m<sup>2</sup>. We used data from an inventory carried out in a forest unit (Bom Futuro National Forest) in the southwestern Brazilian Amazon, where 22 clusters were distributed as a two-stage sampling design. Three products were evaluated: (i) MV of trees with a diameter at breast height (DBH)  $\geq 20$  cm (P1); (ii) MV of trees with DBH  $\geq 50$  cm (P2); and (iii) MV of commercial species with DBH  $\geq 50$  cm and stem quality 'level 1' or 'level 2' (P3). We assessed ten scenarios in which the cluster size was reduced from 8,000 m<sup>2</sup> to 800 m<sup>2</sup>. The accuracy of P1, P2 and P3 was highly significantly lower for reductions  $< 2,400$  m<sup>2</sup>. The precision was more sensitive to variations in cluster size, especially for P2 and P3. Minimum cluster sizes were  $\geq 2,400$  m<sup>2</sup> to estimate P1,  $\geq 4,800$  m<sup>2</sup> to estimate P2, and  $\geq 7,200$  m<sup>2</sup> to estimate P3. We concluded that it is possible to reduce the cluster size without losing the accuracy and precision given by the original NFI cluster. A cluster of 2,400 m<sup>2</sup> provides estimates as accurate as the original cluster, regardless of the evaluated product.

**KEYWORDS:** National Forest Inventory, merchantable volume, precision, accuracy, Amazonian timber species

## Avaliando a redução do tamanho do conglomerado para estimar o volume de madeira em uma floresta amazônica

### RESUMO

Enquanto o Inventário Florestal Nacional Brasileiro (IFN) está em andamento, há uma demanda crescente para entender o efeito da área do conglomerado sobre a exatidão e precisão da estimativa de atributos florestais. O objetivo deste estudo foi determinar a área mínima de um conglomerado para estimar o volume comercial (VC) com a mesma acurácia e precisão que as estimativas derivadas do conglomerado original de 8.000 m<sup>2</sup>. A base de dados é proveniente de um inventário realizado em uma unidade florestal (Floresta Nacional do Bom Futuro) no sudoeste da Amazônia brasileira, onde 22 conglomerados foram distribuídos em um desenho amostral em dois estágios. Foram avaliados três produtos: (i) VC de árvores com diâmetro à altura do peito (DAP)  $\geq 20$  cm (P1); (ii) VC de árvores com DAP  $\geq 50$  cm (P2); e (iii) VC de espécies comerciais com DAP  $\geq 50$  cm e qualidade de fuste 'nível 1' ou 'nível 2' (P3). O estudo avaliou dez cenários em que a área do conglomerado foi reduzida de 8.000 a 800 m<sup>2</sup>. A acurácia de P1, P2 e P3 foi significativamente menor para reduções  $< 2.400$  m<sup>2</sup>. A precisão foi mais sensível à variação no tamanho do conglomerado, sobretudo para P2 e P3. Os tamanhos mínimos de conglomerado foram  $\geq 2.400$  m<sup>2</sup> para estimar P1,  $\geq 4.800$  m<sup>2</sup> para estimar P2 e  $\geq 7.200$  m<sup>2</sup> para estimar P3. Concluímos que é possível reduzir a área do conglomerado sem perder acurácia e precisão do conglomerado original do IFN. Um conglomerado de 2.400 m<sup>2</sup> fornece estimativas com a mesma acurácia que o conglomerado original, independentemente do produto avaliado.

**PALAVRAS-CHAVE:** Inventário Florestal Nacional, volume comercial, precisão, acurácia, espécies madeireiras amazônicas

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## INTRODUCTION

Forest inventories are the main tool to quantify and characterize forest resources and their composition, providing useful information to forest management, conservation, and policy (Tomppo *et al.* 2010). Based on the degree of coverage, the inventories can be classified either as complete, when the entire forest is measured (i.e., a census), or incomplete, when only a forest sample is evaluated (Loetsch *et al.* 1973). In the latter case, a representative sample is crucial, which depends on distinct factors, such as the dimension of sampling units and the sampling design, which define the precision of estimates.

Increasing forest inventory efficiency is a trade-off between attaining higher accuracy and precision, and seeking practices that allow cost reduction (Westfall *et al.* 2011; Westfall *et al.* 2016; Rätty *et al.* 2018). In general, costs are directly related to data detail level and sampling intensity (Druszcz *et al.* 2012), as well as sampling unit area (Westfall *et al.* 2016). Plot area rules the precision and accuracy of estimates of forest attributes, while precision is also dependent on available resources, as field assessments generally are a demanding component of the forest inventory (Westfall *et al.* 2016; Rätty *et al.* 2018; Westfall *et al.* 2019). Therefore, defining minimal sampling effort that ensures both high accuracy and precision in the estimation of variables of interest will increase inventory efficiency (Gregoire and Valentine, 2007; Westfall *et al.* 2016).

The challenge of finding the optimal trade-off between precision/accuracy and sampling effort is intensified in the Brazilian National Forest Inventories (NFIs). The NFI is one of the main surveys carried out by the federal government to produce information on Brazilian forest resources (SFB 2020). In the NFI, the ratio between sampled area and population area is notably smaller than in small-scale inventories. NFI SUs usually are field plots structured as clusters of smaller sub-units (Lawrence *et al.* 2010). These SUs are systematically distributed across the national territory (Westfall *et al.* 2016). The Brazilian NFI SUs usually are clusters of 4,000 or 8,000 m<sup>2</sup>. The preference for clusters is, among other reasons, the lower variation among clusters, thus requiring the use of fewer SUs (Cochran 1977).

There is a growing demand to understand the relationship of cluster size with accuracy and precision of estimates, i.e., what is the effect of sampling unit size on the precision and accuracy of the estimates of merchantable volume? We aimed to estimate the minimum sampling unit size that provides merchantable volume estimates as accurate and precise as the standard NFI sampling unit of 8,000 m<sup>2</sup> used in the Amazon.

## MATERIAL AND METHODS

### Study area

The study area covers about 80% (82,918.33 ha) of the Bom Futuro National Forest (9°27'39.0"S, 63°54'26.4"W),

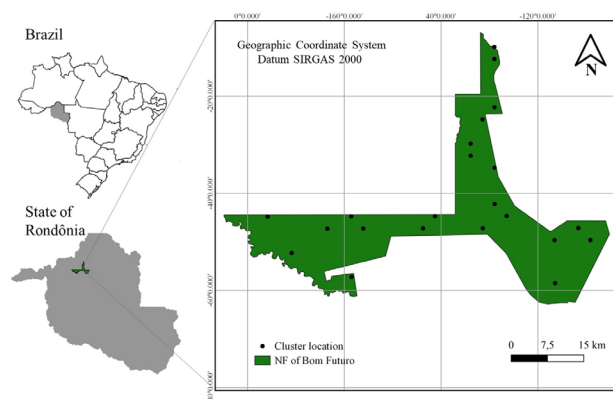
a protected area of native forest partially open for sustainable use, located between the municipalities of Porto Velho and Buritis in the state of Rondônia, Brazil (Wikiparques 2019) (Figure 1). The region has a mean annual precipitation of 2,400 mm and a mean temperature of 25.2 °C. According to the Köppen climate classification, the local climate is Am humid (Alvares *et al.* 2013).

The Bom Futuro National Forest consists of five types of vegetation formations: (i) dense alluvial rainforest (floodplain forest); (ii) dense submontane rainforest; (iii) open ombrophilous forest; (iv) savanna (forested savanna, tree savanna with gallery forest and park savanna with gallery forest); and (v) savanna/rainforest transition. The management area, composed of native forests with economic potential for sustainable management, is predominantly dominated by open forest and dense forest (ICMBio 2019). Both forest types correspond to the predominant typologies in the Amazon Biome (dense rainforest = 41.67%, open rainforest = 20.91%) (MMA 2004).

### Forest inventory and sampling design

Installation of sampling units (SUs) and data collection were performed following the Brazilian NFI guidance, defined by the Brazilian Forestry Service (SFB 2019). The NFI SUs are clusters composed of four crosswise sub-units (as a Maltese cross). Each cluster had 8,000 m<sup>2</sup>, divided into four sub-units of 20 m x 100 m (2,000 m<sup>2</sup>), which is the standard for the Amazon biome. Further details can be found in the NFI manual (SFB 2014).

The sampling design was of two stages. The first was a systematic distribution of points 2.5 km apart from each other, forming a regular grid where each point represented a cell of 6.25 km<sup>2</sup> (2.5 x 2.5 km). These 6.25-km<sup>2</sup> cells correspond to the fourth level of density of the NFI [the first level is 400 km<sup>2</sup> (20 x 20 km), the second 100 km<sup>2</sup> (10 x 10 km), and the third 25 km<sup>2</sup> (5 x 5 km)] (Vibrans *et al.* 2010). The



**Figure 1.** Location of the study area (Bom Futuro National Forest) in the state of Rondônia, Brazil, and the distribution of the 22 sampling clusters within the study area. This figure is in color in the electronic version.

second stage was a random selection of 22 first-stage points to install 22 clusters. The number of clusters was based on a pilot inventory to meet a maximum error of 20% while estimating merchantable volume (MV) of individuals with diameter at breast height (DBH) ≥ 20 cm.

Each standard sub-unit was subdivided into 20 sub-plots of 10 m x 10 m (100 m<sup>2</sup>) (Figure 2). To assess how MV estimates change with decreasing SU area, we performed a stepwise reduction in the SU area by eliminating the last two sub-plots of each sub-unit. Because each SU consists of four sub-units, eight sub-plots (or 800 m<sup>2</sup>) of each SU were removed per reduction. After these successive reductions, the SU areas were: 8,000 m<sup>2</sup> (original area); 7,200 m<sup>2</sup> (first reduction); 6,400 m<sup>2</sup> (second); 5,600 m<sup>2</sup> (third); and so on, until the ninth reduction, i.e., 800 m<sup>2</sup>, which was the smallest area. Since there were nine area reductions plus the original area, our sampling design comprised ten sampling-area sizes (Figure 2, Table 1).

### Wood products

MV was our variable of interest, defined as the wood volume until either the first stem bifurcation or the beginning of a tortuosity or of the tree crown. Equation 1 was used to obtain the individual MV of the trees. This equation comes from the Schumacher-Hall linear model adjusted to the sustainable forest management plan of the Jamari National Forest, located in northeastern Rondônia state and with a similar forest type to that in the Bom Futuro National Forest.

$$\text{Log (MV)} = -3.81800 + 1.92553 \log (\text{DBH}) + 0.66726 \log (\text{HC}) \quad [1]$$

where: DBH = diameter at breast height; HC = commercial height.

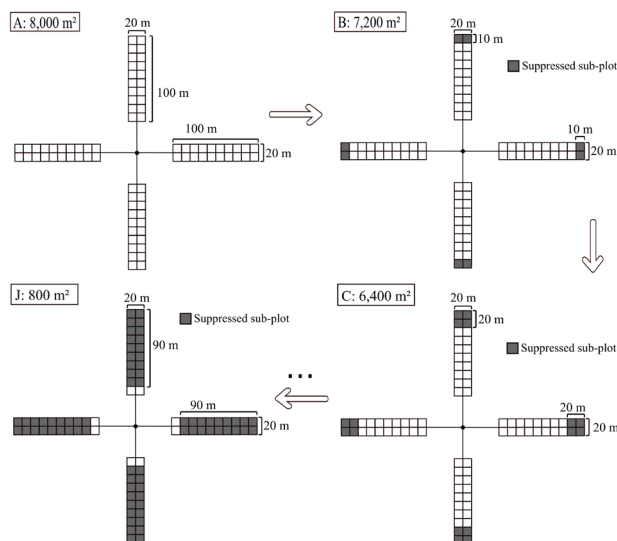
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After estimating individual tree MV, three products (P1, P2 and P3) were assessed. P1 consists of MV of trees with DBH ≥ 20 cm; P2 is MV of trees with DBH ≥ 50 cm; and P3 is MV of commercial species with DBH ≥ 50 cm and stem quality ‘level 1’ (high stem straightness, cylindrical stem, without apparent defects) or ‘level 2’ (moderate stem straightness, cylindrical stem, and with acceptable defects) (see Table 2 for product statistics for 8,000-m<sup>2</sup> SUs).

### Precision and accuracy

We calculated MV (m<sup>3</sup> ha<sup>-1</sup>) of the products per scenario (Figure 2; Table 1; Table 2). We assumed the 8,000-m<sup>2</sup> SU as the benchmark for the MV estimates. The accuracy of each other scenario (Table 1) was evaluated by comparing their MV means to the means of scenario A in the 22 replicates through Student’s t-tests (α = 0.05). The normality of the distribution of MV estimates (α = 0.05) was assessed and confirmed by Kolmogorov-Smirnov tests. The 95% confidence interval (95% CI) of the mean was calculated for all scenarios and products.

The precision of the MV estimates for 800 to 7,200 m<sup>2</sup> relative to 8,000 m<sup>2</sup> was assessed through the coefficient of variation (CV) and the sampling error for each product in the 22 cluster replicates. The sampling error was expressed as the absolute error (E<sub>a</sub>) (Equation 2) and relative error (E<sub>r</sub>) (Equation 3).



**Figure 2.** Diagrams of the sampling design for evaluation of the effect of cluster size on the accuracy and precision of merchantable wood volume estimation in the Bom Futuro National Forest, Rondônia state, Brazil. A – SU with standard dimension of 8,000 m<sup>2</sup>; B – first level of area reduction to a 7,200-m<sup>2</sup> sampling unit; C – second level of area reduction to 6,400 m<sup>2</sup>; J – ninth and maximum level of tested area reduction to a 800-m<sup>2</sup> sampling unit.

**Table 1.** Sampling parameters of different sampling-unit sizes for evaluation of the effect of cluster size on the accuracy and precision of the estimation of merchantable wood volume in the Bom Futuro National Forest, Rondônia state, Brazil.

Scenario	SU (cluster) area (m <sup>2</sup> )	Sampled area (ha)	Sampling intensity (%)	N
A	8,000	17.60	0.0212	22
B	7,200	15.84	0.0191	22
C	6,400	14.08	0.0170	22
D	5,600	12.32	0.0149	22
E	4,800	10.56	0.0127	22
F	4,000	8.80	0.0106	22
G	3,200	7.04	0.0085	22
H	2,400	5.28	0.0064	22
I	1,600	3.52	0.0042	22
J	800	1.76	0.0021	22

N = number of installed Sus; sampling intensity = sampled area (ha) / 82,918.33 ha x 100.

**Table 2.** Characteristics of DBH and wood volume by product (see Material and Methods for product description) in 22 sampling clusters of 8,000-m<sup>2</sup> in the Bom Futuro National Forest, Rondônia state, Brazil.

Product	N	Variable	Mean ± SD	Minimum	Maximum	CV (%)
P1	2,952	DBH (cm)	32.9 ± 15.1	20.0	185.6	45.7
		Wood volume (m <sup>3</sup> )	0.925 ± 1.410	0.065	26.202	152.0
P2	388	DBH (cm)	66.3 ± 17.5	50.1	185.6	26.4
		Wood volume (m <sup>3</sup> )	3.502 ± 2.940	0.472	26.202	83.9
P3	40	DBH (cm)	70.2 ± 21.6	50.4	148.6	30.8
		Wood volume (m <sup>3</sup> )	4.131 ± 3.550	1.341	19.286	86.0

N = number of sampled trees; SD = standard deviation; DBH = diameter at breast height; CV = coefficient of variation

$$(E_a) = t s_x / \sqrt{n} \quad \text{Equation [2]}$$

$$(E_r) = 100 E_a / \bar{x} \quad \text{Equation [3]}$$

where:  $s_x$  the standard deviation of the MV;  $n$  is the number of SUs; and  $t$  is the Student's t-test value.

Scenarios exhibiting a decrease of up to five percentage points in precision in  $E_r$  relative to 8,000-m<sup>2</sup> clusters were considered to display a precision in the MV estimates equivalent to that of the standard SU.

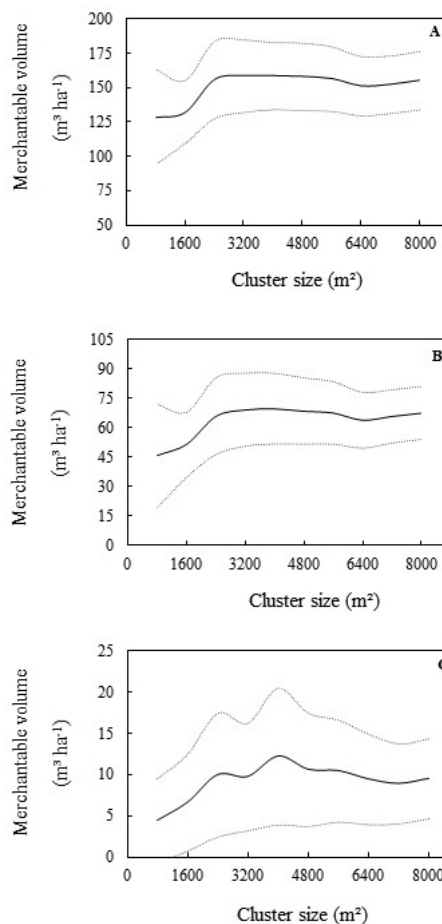
## RESULTS

Mean MV varied from 158.5 to 128.7 m<sup>3</sup> ha<sup>-1</sup> for P1, 69.6 to 45.6 m<sup>3</sup> ha<sup>-1</sup> for P2, and 12.3 to 4.40 m<sup>3</sup> ha<sup>-1</sup> for P3 (Figure 3). SUs of 4,000 m<sup>2</sup> produced the highest means in all products, while SUs of 800 m<sup>2</sup> produced the lowest. The means for all products were very similar for SUs with areas ≥ 2,400 m<sup>2</sup>.

The 95% CI remained relatively constant with increasing SU area, except for 800-m<sup>2</sup> SUs, in which the CI was wider, thus the uncertainty greater than for the other scenarios (Figure 3). P3 in 800-m<sup>2</sup> SUs had a negative lower limit of the CI, which was owed to the low density of trees of commercial value with DBH ≥ 50 cm in forest stands, which made them vary scarce in the sampled areas of 800-m<sup>2</sup> SUs (Figure 2; Table 1).

MV for P1 and P2 did not differ significantly from scenario A (original SU area of 8,000 for m<sup>2</sup>) for areas ≥ 2,400 m<sup>2</sup> (Table 3). Accordingly, the 95% CI tended to be more stable around the mean from 2,400 m<sup>2</sup> onwards (Figure 3). For P3, the MV of SU areas of 1,600 m<sup>2</sup> or larger did not differ significantly from the original SU area (Table 3).

For P1 and P2, we observed a strong trend towards the stabilization of the  $E_r$  of the MV in SUs ≥ 1,600 m<sup>2</sup> (Figure 4b). The  $E_r$  for P3 decreased constantly with the increase of SU area, while  $E_a$  did not vary noticeably, unlike it did for P1

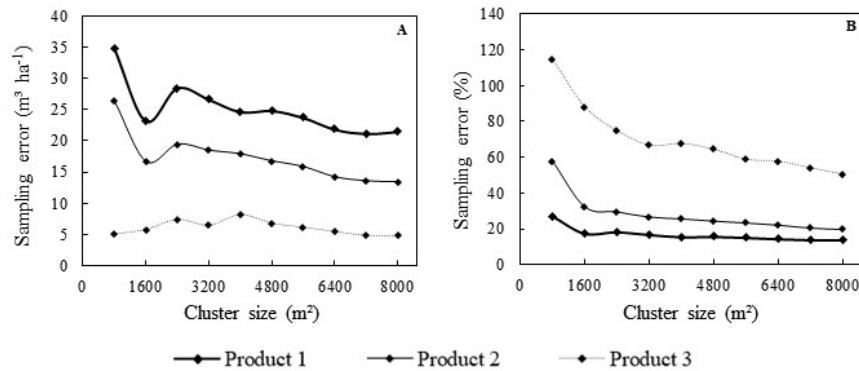


**Figure 3.** Mean (solid line) and 95% confidence interval (dotted lines) for the estimation of merchantable wood volume in sampling areas of different size for Product 1 (A), Product 2 (B) and Product 3 (C) in Bom Futuro National Forest, Rondônia, Brazil. Means are based on 22 cluster replicates.

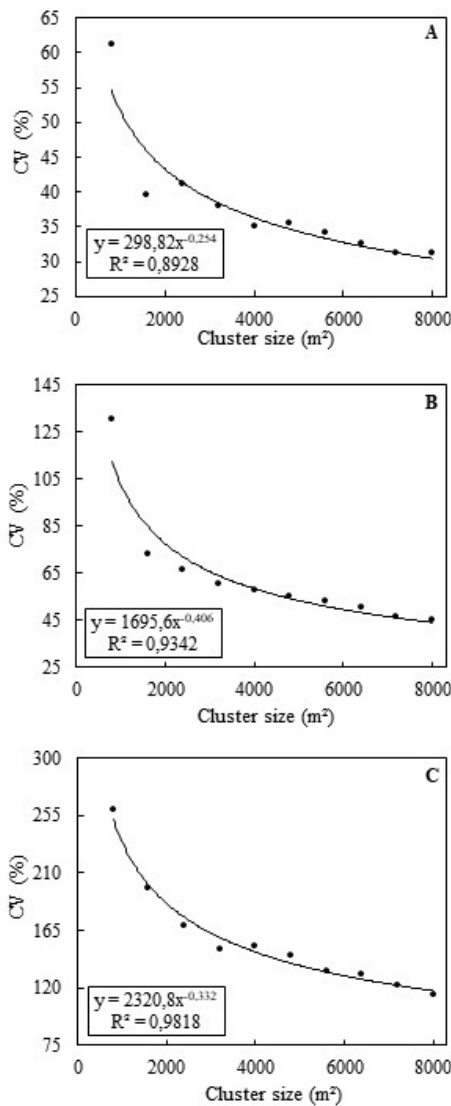
and P2 between 800 and 1,600 m<sup>2</sup> (Figure 4a). The product with the highest  $E_a$  presented the lowest  $E_r$  and vice-versa (Figure 4a).

Adopting a SU of 2,400 m<sup>2</sup> to estimate P1 resulted in a precision loss of 4.4% relative to the 8,000-m<sup>2</sup> SU ( $E_r$  increased from 13.9% to 18.3%, Figure 4b). For P2, using a SU of 4,800 m<sup>2</sup> resulted in an error increase from 19.9% to 24.5% (4.6% increase, Figure 4b). The precision was reduced in 3.4% when using a SU of 7,200 m<sup>2</sup> for P3 ( $E_r$  increased from 50.6% to 54%, Figure 4b).

The relationship between CV and SU area followed a negative exponential trend for the three products (Figure 5). The CV is linked to the abundance of each product in the sampled area, thus the largest variation range was observed for the least abundant product (P3) (120 to 260%), while P2 had the intermediate range (50 to 130%), and P1, being the most abundant product, exhibited the smallest range (34 to 64%). As P2 is less abundant than P1, its CV was 1.5 to 2.5



**Figure 4.** Relationship between cluster size and absolute sampling error (A) and relative sampling error (B) of merchantable wood volume estimates in sampling areas of different size for Product 1, Product 2, and Product 3 in Bom Futuro National Forest, Rondônia, Brazil. Points are the mean of 22 replicates.



**Figure 5.** Relationship between cluster size and coefficient of variation of merchantable wood volume estimates in sampling areas of different size for Product 1 (A), Product 2 (B) and Product 3 (C) in Bom Futuro National Forest, Rondônia, Brazil. Points are the mean of 22 replicates.

**Table 3.** T-test values for comparison of mean merchantable wood volume ( $m^3 ha^{-1}$ ) estimated for a standard cluster size of  $8,000 m^2$  with nine levels of cluster-size reduction for Product 1, Product 2 and Product 3 (see Material and Methods) in Bom Futuro National Forest, Rondônia, Brazil. P-values in bold indicate statistically significant comparisons.

Comparison	Product 1		Product 2		Product 3	
	t-test	p-value	t-test	p-value	t-test	p-value
$8,000 m^2 \times 7,200 m^2$	0.284	0.7791	0.266	0.793	0.260	0.7973
$8,000 m^2 \times 6,400 m^2$	0.381	0.7068	0.555	0.585	<b>0.027</b>	0.9788
$8,000 m^2 \times 5,600 m^2$	-0.115	0.9092	-0.014	0.989	-0.412	0.6845
$8,000 m^2 \times 4,800 m^2$	-0.266	0.7928	-0.159	0.875	-0.484	0.6335
$8,000 m^2 \times 4,000 m^2$	-0.321	0.7515	-0.345	0.734	-1.179	0.2514
$8,000 m^2 \times 3,200 m^2$	-0.312	0.7579	-0.261	0.797	-0.103	0.9192
$8,000 m^2 \times 2,400 m^2$	-0.049	0.9610	0.256	0.800	-0.201	0.8429
$8,000 m^2 \times 1,600 m^2$	2.212	<b>0.0382</b>	2.494	<b>0.021</b>	1.257	0.2224
$8,000 m^2 \times 800 m^2$	2.557	<b>0.0184</b>	3.384	<b>0.003</b>	2.211	<b>0.0382</b>

times higher than that of P1. Likewise, P3 exhibited a CV two to three times higher than that of P2.

## DISCUSSION

### Minimum sampling-unit size

Our objective was to determine the minimum SU size that estimates the MV as accurately and precisely as the  $8,000\text{-}m^2$  standard SU in an area of Amazon rainforest, which resulted to be  $2,400 m^2$  for P1,  $4,800 m^2$  for P2, and  $7,200 m^2$  for P3.

Considering accuracy as the only criterion to choose the minimum SU size, an area of  $2,400 m^2$  would be suitable for all products. However, given the observed variation in precision, additional caution is needed in the assessment of minimum SU size. Sampling errors directly affect the confidence interval of an estimate. The larger the error in an estimate, the wider the confidence interval, and vice-versa (Loetsch *et al.* 1973; Péllico Netto and Brena 1997). Although  $E_r$  and  $E_a$  are complementary to each other,  $E_r$  has greater applicability in practical terms (Cavalcanti *et al.* 2009;

Cavalcanti *et al.* 2011; Oliveira *et al.* 2014). Specifically,  $E_a$  lacks information about the magnitude of its value relative to the mean. For example, an absolute error of  $20 \text{ m}^3 \text{ ha}^{-1}$  for a mean of  $40 \text{ m}^3 \text{ ha}^{-1}$  corresponds to a relative error of 50%, which is considered high in forest inventories. Conversely, for this same absolute error, but with a mean of  $200 \text{ m}^3 \text{ ha}^{-1}$ , the relative error would be only 10%, which is acceptable for most inventories.

In a similar study in an area of Amazon forest in Pará state, Flores *et al.* (2012) evaluated the effect of distance between clusters and among sub-plots within clusters on three products based on total wood volume of trees with DBH  $\geq 30 \text{ cm}$  (77 forestry species, ten most abundant species, and ten most commercialized species), and concluded that the  $8,000\text{-m}^2$  cluster is efficient in estimating the analyzed products. Likewise, Queiroz *et al.* (2011) also concluded that a  $8,000\text{-m}^2$  Maltese-cross cluster was efficient in estimating three wood-volume products (DBH  $\geq 25 \text{ cm}$ ) in the Tapajós Natinal Forest, also in Pará state (all species, species with an international market, and only *Manilkara huberi* (Ducke) Standl). Our study showed that it is possible to reduce the SU area while attaining similar accuracy and precision as with an  $8,000\text{-m}^2$  cluster, allowing to reduce inventory costs while obtaining reliable MV estimates.

The recommendations of a larger SU by Queiroz *et al.* (2011) and Flores *et al.* (2012) is due to their use of the maximum curvature method to obtain the minimum SU size, which is a method based on the stabilization of the coefficient of variation. Our results also indicate that the coefficients of variation tend to stabilize with SUs  $\sim 8,000 \text{ m}^2$ , however, we did not aim to determine the SU size that stabilizes the MV estimation by using the maximum curvature method, not to determine where the coefficient of variation stabilizes, since  $8,000 \text{ m}^2$  was the largest SU area evaluated.

### Effect of sampling-unit area on merchantable volume

Cavalcanti *et al.* (2009) assessed the effect of SU area on the precision and accuracy of inventories in the Amazon forest through the MV of trees with DBH  $\geq 40 \text{ cm}$ , and noted an exponential decrease in MV variation as SU area increased, which was also observed by Flores *et al.* (2012) in our study. Cavalcanti *et al.* (2009) tested SU areas ranging from  $2,500$  to  $20,000 \text{ m}^2$  and found that the coefficient of variation tended to stabilize with SUs  $\geq 7,500 \text{ m}^2$ , which was also observed in our study, with a stabilization in the coefficient of variation of P1 at SUs  $\geq 7,200 \text{ m}^2$ .

Flores *et al.* (2012) found a range of coefficients of variation comparable to our results, with  $\sim 100\text{--}150\%$  for the most abundant product,  $\sim 130\text{--}200\%$  for intermediate abundance, and  $\sim 140\text{--}240\%$  for the less abundant product. Likewise, Queiroz *et al.* (2011) also observed coefficients of

variation ranges of  $\sim 100\%$ ,  $\sim 100\text{--}300\%$ , and  $\sim 150\text{--}450\%$ , respectively for the most, intermediate, and less abundant products.

Similar to Flores *et al.* (2012) and Queiroz *et al.* (2011), we also observed that scarcer products and smaller SUs resulted in larger coefficients of variation. The high coefficients of variation were caused by the high errors observed in P3 and, less intensely, by the errors in P2 and P1. As the abundance of each product varies with the successional stage and disturbance state of the forest, our recommendation applies to forests with products of similar abundance to those evaluated in here.

### Sampling intensity and merchantable volume

The sampling intensity of  $0.0212\%$  adopted in our study for the  $8,000\text{-m}^2$  cluster sufficed to meet the minimum precision of 20% for P1 and P2 (see Figure 4b). If more precise estimates are required, a higher sampling intensity would likely be necessary. For example, in the study conducted by Cavalcanti *et al.* (2011) in an Amazon forest, a sampling intensity of 14% ( $\sim 660\times$  greater than  $0.0212\%$ ) was needed to meet a precision of  $\sim 8\%$  of the MV of commercial species of trees with DBH  $\geq 40 \text{ cm}$ . Thus, the sampling intensity adopted in our study may be too low to achieve an error smaller than 10%, especially for scarcer products such as P2 and P3. In a study on the effect of SU size on tree wood and carbon-stock estimates in an Amazonian forest, Oliveira *et al.* (2014) found best results with SUs  $\geq 1,200 \text{ m}^2$  for DBH  $\geq 20 \text{ cm}$ , with mean uncertainty of 9.07%, and with SUs between  $2,000 \text{ m}^2$  and  $3,000 \text{ m}^2$  for DBH  $\geq 25 \text{ cm}$ , with mean uncertainty of 6.37%. These results also corroborate our findings that the increase of SU area increases precisions.

Andrade *et al.* (2015) also evaluated tree-volume estimates with varying SU area [ $1,500 \text{ m}^2$  ( $30 \text{ m} \times 50 \text{ m}$ ) for DBH  $10\text{--}25 \text{ cm}$ ,  $3,000 \text{ m}^2$  ( $30 \text{ m} \times 100 \text{ m}$ ) for DBH  $25\text{--}50 \text{ cm}$ , and  $7,500 \text{ m}^2$  ( $30 \text{ m} \times 250 \text{ m}$ ) for DBH  $\geq 50 \text{ cm}$ ] and obtained an error smaller than 10% for the volume of trees with DBH  $\geq 10 \text{ cm}$  and trees with DBH  $\geq 50 \text{ cm}$ . This accuracy was considerably higher than that observed in our study, which may be due to the higher sampling intensity ( $\sim 10$  times higher) in the study by Andrade *et al.* (2015) and shows that sampling intensity is directly related to inventory accuracy. Since the intensity depends on the area and number of SUs, it is expected that more SUs will contribute to improve the accuracy.

We evaluated the effect of SU area while keeping SU number fixed. An alternative approach would be to assess SU area reduction and to vary the number of SUs (e.g., Kauai *et al.* 2019). Varying SU area usually has a different effect than varying number of SUs (Oliveira *et al.* 2014). For example, in forest remnants of an ombrophilous forest in southern Brazil, gains in precision on the basal area estimation were less evident when varying SU area than when varying number of SUs (Augustynczyk *et al.* 2013). Future studies should address

both number of SUs and SU area, as well as other variables of interest, to improve our ability to increase the efficiency of forest inventories.

## CONCLUSIONS

Our results indicate that smaller clusters could replace the original standard 8,000-m<sup>2</sup> cluster for forest inventory estimates in Amazon rainforest without losing precision and accuracy of merchantable volume estimation. We found that the minimum sampling unit size to estimate merchantable volume is 2,400 m<sup>2</sup> for trees with DBH ≥ 20 cm, 4,800 m<sup>2</sup> for trees with DBH ≥ 50 cm, and 7,200 m<sup>2</sup> for commercial species with DBH ≥ 50 cm and stem quality of level 1 or 2. The precision of the estimates was affected more strongly by reduction of cluster size than accuracy. Regardless of the wood product abundance in the forest, a cluster size of 2,400 m<sup>2</sup> yielded estimates as accurate as those of the original standard cluster of 8,000 m<sup>2</sup>. Precision, however, was dependent on cluster size and product abundance. We encourage other researchers to further assess the relationship between cluster size and accuracy and precision of other variables of interest of the Brazilian NFI, focusing on determining smaller yet reliable cluster sizes for wood product estimates.

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